

Snapshot:

Calculus

①

Classwork: Simplify and find a and b

$$(\sqrt{13-4\sqrt{3}})^2 = (a + b\sqrt{3})^2$$

$$13 - 4\sqrt{3} = a^2 + 2(a)(b\sqrt{3}) + b^2 \cdot 3$$

$$\underline{13} - \underline{4\sqrt{3}} = \underline{a^2} + \underline{2ab\sqrt{3}} + \underline{3b^2}$$

$$i) a^2 + 3b^2 = 13 \quad ii) 2ab\sqrt{3} = -4\sqrt{3}$$

* solve for a in terms of b

wisest:

$$\frac{2ab\sqrt{3}}{2b\sqrt{3}} = \frac{-4\sqrt{3}}{2b\sqrt{3}}$$

$$a = \frac{-2}{b}$$

← use this to substitute into equation i

$$a = \frac{-2}{b} \leftarrow \text{substitute to get } b. \text{ (2)}$$

$$i) a^2 + 3b^2 = 13$$

$$\left(\frac{-2}{b}\right)^2 + 3b^2 = 13$$

$$ii) 2ab\sqrt{3} = -4\sqrt{3}$$

$$b^2 \left(\frac{4}{b^2} + 3b^2 \right) = (13)b^2 \leftarrow \text{get rid of fraction}$$

$$\frac{4b^2}{b^2} + 3b^4 = 13b^2$$

$$4 + 3b^4 = 13b^2 \leftarrow \text{set equal to } 0$$
$$-13b^2 \quad -13b^2$$

$$4 + 3b^4 - 13b^2 = 0 \leftarrow \text{rearrange}$$

$$3b^4 - 13b^2 + 4 = 0 \leftarrow \text{substitute: } x = b^2$$

$$\downarrow$$
$$3x^2 - 13x + 4 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{13 \pm \sqrt{169 - 48}}{6} = \frac{13 \pm \sqrt{121}}{6} = \frac{13 \pm 11}{6}$$

$$x = \frac{13 \pm \sqrt{121}}{6}$$

3

$$x = \frac{13 \pm 11}{6}$$

$$x = \frac{13+11}{6}$$

$$x = \frac{13-11}{6}$$

$$x = \frac{24}{6}$$

$$x = \frac{2}{6}$$

$$x = 4$$

$$x = \frac{1}{3}$$

Recall: $x = b^2$

$$x = 4$$

↓

$$b^2 = 4$$

$$b = \pm 2$$

$$x = \frac{1}{3}$$

↓

$$b^2 = \frac{1}{3}$$

$$b = \pm \frac{1}{\sqrt{3}}$$

$$a = \frac{-2}{b}$$

Substitute b to find a .

Sol. 1

$$b = 2$$

$$a = -\frac{2}{b}$$

$$a = -\frac{2}{2}$$

$$a = -1$$

$$a = -1, b = 2$$

Sol. 2

$$b = -2$$

$$a = -\frac{2}{b}$$

$$a = \frac{-2}{-2}$$

$$a = 1$$

$$a = 1, b = -2$$

Sol. 3

$$b = \frac{1}{\sqrt{3}}$$

$$a = -\frac{2}{b}$$

$$a = \frac{-2}{\left(\frac{1}{\sqrt{3}}\right)}$$

$$a = \left(\frac{-2}{1}\right) \cdot \left(\frac{1}{\sqrt{3}}\right)$$

$$a = \frac{-2 \cdot \sqrt{3}}{1 \cdot 1}$$

$$a = \frac{-2\sqrt{3}}{1}$$

$$a = -2\sqrt{3}$$

$$a = -2\sqrt{3}, b = \frac{1}{\sqrt{3}}$$

Sol. 4 ④

$$b = -\frac{1}{\sqrt{3}}$$

$$a = -\frac{2}{b}$$

$$a = \frac{-2}{\left(-\frac{1}{\sqrt{3}}\right)}$$

$$a = \frac{-2}{1} \cdot \frac{1}{-\frac{1}{\sqrt{3}}}$$

$$a = \frac{2 \cdot \sqrt{3}}{1 \cdot 1}$$

$$a = 2\sqrt{3}$$

$$a = 2\sqrt{3}, b = -\frac{1}{\sqrt{3}}$$

Sol 1

$$a = -1, b = 2$$

Check if true:

$$\sqrt{13-4\sqrt{3}} = a + b\sqrt{3}$$

$$\left(\sqrt{13-4\sqrt{3}}\right)^2 = \left(\overset{\downarrow}{-1} + \overset{\downarrow}{2\sqrt{3}}\right)^2$$

$$13 - 4\sqrt{3} = 1 + 2(-1)(2\sqrt{3}) + 4 \cdot 3$$

$$13 - 4\sqrt{3} = 1 - 4\sqrt{3} + 12$$

$$13 - 4\sqrt{3} = 13 - 4\sqrt{3}$$



Sol 2

5

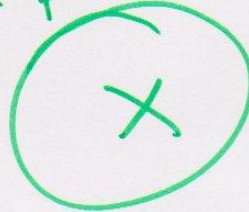
$$a = 1, b = -2$$

$$\sqrt{13-4\sqrt{3}} = a + b\sqrt{3}$$

$$= 1 - 2\sqrt{3}$$

negative

Doesn't work, needs to be a positive number.



Sol 3

$$a = -2\sqrt{3}, b = \frac{1}{\sqrt{3}}$$

$$\sqrt{13-4\sqrt{3}} = -2\sqrt{3} + \frac{1}{\sqrt{3}}\sqrt{3}$$

$$= -2\sqrt{3} + 1$$

negative



Sol 4

$$a = 2\sqrt{3}, b = -\frac{1}{\sqrt{3}}$$

$$\sqrt{13-4\sqrt{3}} = +2\sqrt{3} - \frac{1}{\sqrt{3}}\sqrt{3}$$

$$= 2\sqrt{3} - 1$$



same as first solution.

Classwork / Homework :

Simplify the following square roots:

$$\textcircled{1} \sqrt{7 - 4\sqrt{3}}$$

$$\textcircled{2} \sqrt{6 + 2\sqrt{5}}$$

Study for tomorrow's quiz!